

## Seminar 4

**(S4.1)** Let  $N = (D, c, s, t)$  be a flow network with the property that all capacities are even natural numbers. Prove that the value of the maximum flow is even.

**(S4.2)** Let  $D = (V, A)$  be a digraph. Assume that  $v \in V$  and  $f_1, \dots, f_n : A \rightarrow \mathbb{R}$  are mappings satisfying the flow conservation law at  $v$ . Then any linear combination of  $f_1, \dots, f_n$  satisfies the flow conservation law at  $v$ .

**(S4.3)** Prove Proposition 3.4.2..

**(S4.4)** For any  $s$ - $t$  path  $P$  in  $D$ , prove that  $\chi^P$  satisfies the flow conservation law at every  $v \neq s, t$  and that  $\text{value}(\chi^P) = 1$ .