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## Seminar 2

(S2.1) Let  $C_n = \{x \in \mathbb{R}^n \mid 0 \le x_i \le 1 \text{ for all } i = 1, ..., n\}$  be the unit cube in  $\mathbb{R}^n$  and F be the intersection of  $C_n$  with the hyperplane  $\{x \in \mathbb{R}^n \mid x_n = 1\}$ . What are the dimensions of  $C_n$  and F?

(S2.2) List all faces of the square  $P = \{x \in \mathbb{R}^2 \mid 0 \le x_i \le 1 \text{ for } i = 1, 2\}.$ 

Let  $A \in \mathbb{R}^{m \times n}$ ,  $b \in \mathbb{R}^m$  and  $P = \{x \in \mathbb{R}^n \mid Ax \leq b\}$  be a nonempty polyhedron.

(S2.3) The following are equivalent for every  $y \in \mathbb{R}^n, y \neq 0$ :

(i) 
$$y \in \text{lin.space}(P)$$
.

- (ii) For every  $x \in P$ , the line  $L_{x,y} \subseteq P$ .
- (iii) There exists  $x \in P$  such that  $L_{x,y} \subseteq P$ .

(S2.4) Let F be a face of a polyhedron P. Then F is again a polyhedron. Furthermore, a subset  $F' \subseteq F$  is a face of P if and only if it is face of F.